

1

During a single fission event of uranium-235 in a nuclear reactor the total mass lost is 0.23 u. The reactor is 25% efficient.

How many events per second are required to generate 900 MW of power?

- A  $1.1 \times 10^{14}$
- B  $6.6 \times 10^{18}$
- C**  $1.1 \times 10^{20}$
- D  $4.4 \times 10^{20}$

Handwritten calculations:

$$1.661 \times 10^{-27} \times 0.23 \times c^2$$

$$3.44 \times 10^{-11} \text{ J/event}$$

$$\text{no of events} = \frac{900 \times 10^6}{3.44 \times 10^{-11}}$$

$$= 2.62 \times 10^{19}$$

but only 25% efficient so  $\times 4$

(Total 1 mark)

2

Uranium-236 undergoes nuclear fission to produce barium-144, krypton-89 and three free neutrons.

What is the energy released in this process?

Nuclide	Binding energy per nucleon / MeV
${}^{236}_{92}\text{U}$	7.5
${}^{144}_{56}\text{Ba}$	8.3
${}^{89}_{36}\text{Kr}$	8.6

- A 84 MeV
- B 106 MeV
- C** 191 MeV
- D 3730 MeV

Handwritten nuclear equation:

$${}^{236}_{92}\text{U} \rightarrow {}^{144}_{56}\text{Ba} + {}^{89}_{36}\text{Kr} + 3\text{p}$$

Handwritten calculation for energy release:

$$236 \times 7.5 \rightarrow 144 \times 8.3 + 89 \times 8.6$$

$$1770 \rightarrow 1195.2 + 765.4$$

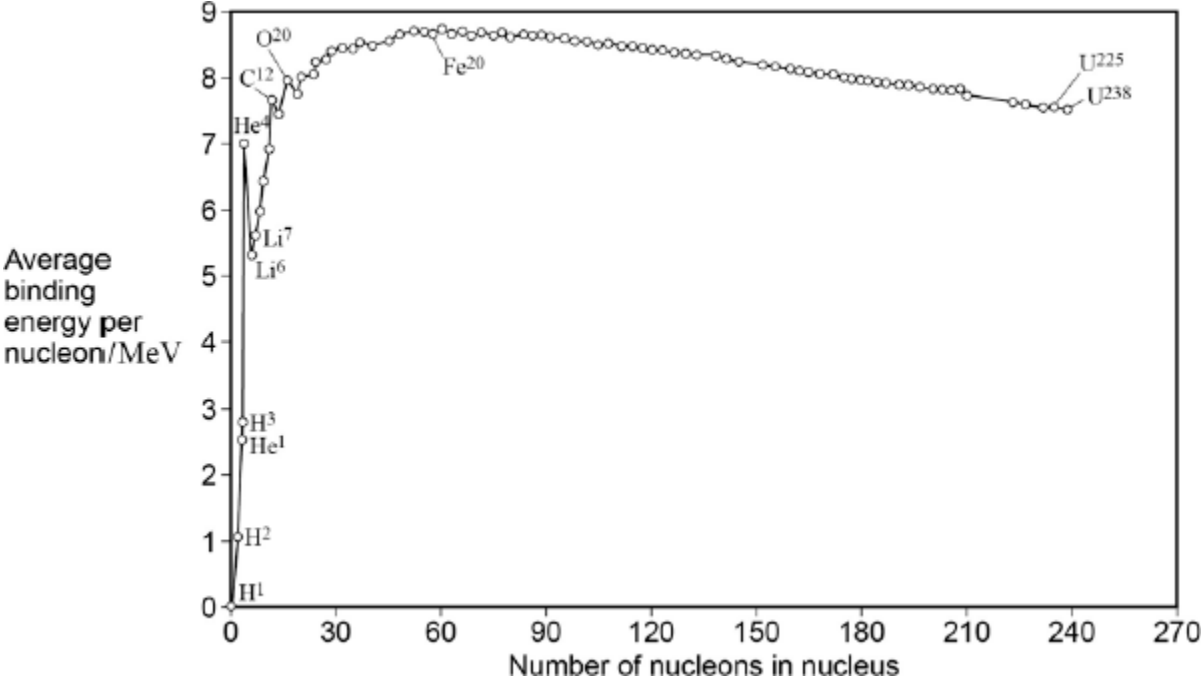
$$\Delta = 190.6 \text{ MeV}$$

not bonded

(Total 1 mark)

3

The graph shows how the binding energy per nucleon varies with the nucleon number for stable nuclei.



What is the approximate total binding energy for a nucleus of  ${}^{184}_{74}\text{W}$ ?

- A 1.28 pJ
- B 94.7 pJ
- C 103 pJ
- D 230 pJ**

8 MeV/nucleon  
Jo  $8 \times 10^6 \times 184 \times 1.6 \times 10^{-19}$

(Total 1 mark)

4

(a) Scattering experiments are used to investigate the nuclei of gold atoms. In one experiment, alpha particles, all of the same energy (monoenergetic), are incident on a foil made from a single isotope of gold.

(i) State the main interaction when an alpha particle is scattered by a gold nucleus.

electrostatic

(1)

(ii) The gold foil is replaced with another foil of the same size made from a mixture of isotopes of gold. Nothing else in the experiment is changed.

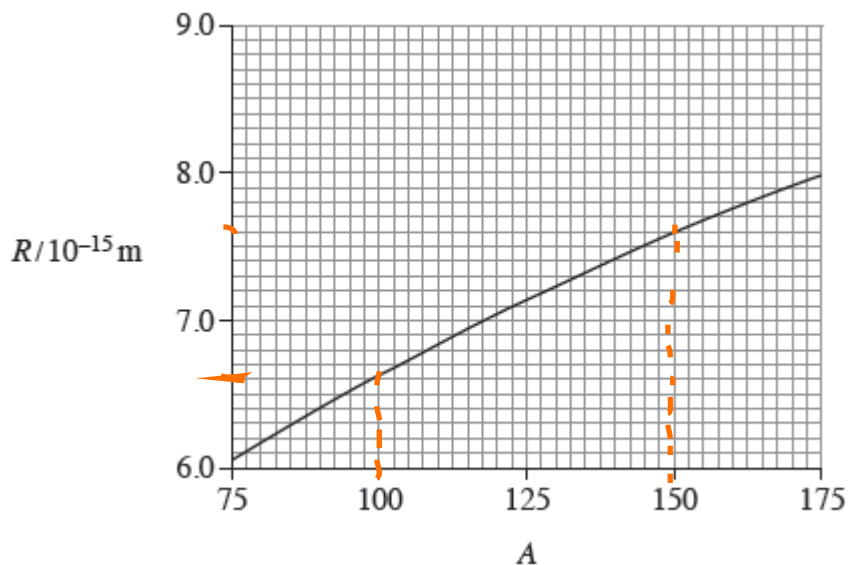
Explain whether or not the scattering distribution of the monoenergetic alpha particles remains the same.

depends!  
→ no change ∴ same charge on nucleus

→ but slightly differing mass which means the recoil of heavy nucleus will slightly less.

(1)

- (b) Data from alpha-particle scattering experiments using elements other than gold allow scientists to relate the radius  $R$ , of a nucleus, to its nucleon number,  $A$ . The graph shows the relationship obtained from the data in a graphical form, which obeys the relationship  $R = r_0 A^{1/3}$



$$\frac{R}{A^{1/3}} = r_0$$

- (i) Use information from the graph to show that  $r_0$  is about  $1.4 \times 10^{-15}$  m.

$r_0$  is gradient

$$\frac{\Delta R}{\Delta A^{1/3}} = \frac{7.6 - 6.6 \times 10^{-15}}{150^{1/3} - 100^{1/3}}$$

$$\approx 1.49 \times 10^{-15}$$

(1)

- (ii) Show that the radius of a  ${}_{23}^{51}\text{V}$  nucleus is about  $5 \times 10^{-15}$  m.

$$R = r_0 A^{1/3} = \frac{1.4 \times 10^{-15} \times 51^{1/3}}{1} = 5.2 \times 10^{-15} \text{ m}$$

(2)

(c) Calculate the density of a  ${}_{23}^{51}\text{V}$  nucleus.

$$r = 5 \times 10^{-15} \quad \rho = \frac{m}{V}$$

State an appropriate unit for your answer.

$$\frac{(23 \times m_p + 28 m_n)}{\frac{4}{3} \pi (5 \times 10^{-15})^3} = 8.5 \times 10^{17}$$

density  $1.6 \times 10^{17}$  unit  $\text{kg/m}^3$

(3)

(Total 8 marks)

## Mark schemes

- 1** C [1]
- 2** C [1]
- 3** D [1]
- 4** (a) (i) electromagnetic / electrostatic / Coulomb (repulsion between the alpha particles and the nuclei) ✓  
*The interaction must be named not just described.* 1
- (ii) the scattering distribution remains the same (because the alpha particles interact with a nucleus) whose charge / proton number / atomic number remains the same or the (repulsive) force remains the same  
*The mark requires a described distribution and the reason for it.*
- Or  
the scattering distribution changes / becomes less distinct because there is a mixture of nuclear masses (which gives a mixture of nuclear recoils) ✓ (owtte)  
*A reference must be made to mass and not density or size.* 1
- (b) (i) use of graph to find  $r_0$   
e.g.  $r_0 = 6.0 \times 10^{-15} / 75^{1/3}$  ✓  
(or  $8.0 \times 10^{-15} / 175^{1/3}$ )  
(  $r_0 = 1.43 \times 10^{-15}$  m)  
*Substitution and calculation t must be shown.*  
*Condone a gradient calculation on R against A<sup>1/3</sup> graph (not graph in question) as  $R \propto A^{1/3}$*  1
- (ii) **Escalate if clip shows  ${}_{13}^{27}\text{Al}$  in the question giving  $R \approx 4 \times 10^{-15}$  m.**  
  
(using  $R = r_0 A^{1/3}$ )  
 $R = 1.43 \times 10^{-15} \times 51^{1/3}$  ✓  
 $R = 5.3 \times 10^{-15}$  (m) ✓  
( $R = 5.2 \times 10^{-15}$  m from  
 $r_0 = 1.4 \times 10^{-15}$  m)  
*First mark for working.*  
*Second mark for evaluation which must be 2 or more sig figs allow CE from (i)  $R = 3.71 \times (i)$ .*  
**Possible escalation.**

- (c) Escalate if clip shows  $\frac{27}{13}$  in the question and / or the use of 27 in the working.

density = mass / volume

$$m = 51 \times 1.67 \times 10^{-27}$$

$$= 8.5 \times 10^{-26} \text{ kg}$$

*Give the first mark for substitution of data into the top line or bottom line of the calculation of density.*

$$v = \frac{4}{3}\pi (5.3 \times 10^{-15})^3$$

$$(6.2(4) \times 10^{-43} \text{ m}^3)$$

*In the second alternative the mark for the substitution is only given if the working equation is given as well.*

Or

$$\text{density} = A \times u / \frac{4}{3}\pi (r_0 A^{1/3})^3$$

$$= u / \frac{4}{3}\pi (r_0)^3$$

*51 × 1.67 × 10<sup>-27</sup> would gain a mark on its own but 1.66 × 10<sup>-27</sup> would need u / 4/3 π(r<sub>0</sub>)<sup>3</sup> as well to gain the mark.*

$$\text{top line} = 1.66 \times 10^{-27}$$

$$\text{bottom line} = \frac{4}{3}\pi (1.43 \times 10^{-15})^3$$

✓ for one substitution

$$\text{density} = 1.4 \times 10^{17} \checkmark$$

$$(1.37 \times 10^{17})$$

$$\text{kg m}^{-3} \checkmark$$

*Expect a large spread of possible answers. For example  
If  $R = 5 \times 10^{-15}$   $V = 5.24 \times 10^{-43}$  and density =  $1.63 \times 10^{17}$ .*

**Possible escalation.**

3

[8]