12 A student aligns the longer edge of a rectangular glass block along a line LR, as shown in Figure 1.

Figure 1


The student marks the outline of the block and directs a ray along PQ.
The student marks the direction of the emergent ray then removes the block and marks a line perpendicular to LR where PQ and LR intersect.

The student then marks the points $\mathbf{W}, \mathbf{X}, \mathbf{Y}$ and $\mathbf{Z}$ that are defined in Figure 2.

Figure 2

(a) Show that the refractive index $n$ of the block is given by the equation

$$
n=\frac{\mathrm{XZ} \times \mathrm{WY}}{\mathrm{YZ} \times \mathrm{WX}}
$$

You may wish to use the equation $n=\frac{\sin \theta_{1}}{\sin \theta_{2}}$
where $\theta_{1}$ and $\theta_{2}$ are the angles shown in Figure 3.
You may also wish to illustrate your answer with a diagram.
Figure 3

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(b) The student repeats the procedure for different directions of the incident ray PQ. The student measures $\mathbf{X Z}, \mathbf{W X}, \mathbf{Y Z}$ and $\mathbf{W Y}$ for each direction of $\mathbf{P Q}$.
State and explain how the student can use these results to obtain a value of $n$ by a graphical method.
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$\qquad$
(c) The student used a block with dimensions $114 \mathrm{~mm} \times 65 \mathrm{~mm} \times 19 \mathrm{~mm}$ to perform the experiment.

The student's data are shown in the table below.

| $\mathbf{W X / m m}$ | $\mathbf{W Y / m m}$ | $\mathbf{X Z} / \mathbf{m m}$ | $\mathbf{Y Z} / \mathbf{m m}$ |
| :---: | :---: | :---: | :---: |
| 130 | 78 | 113 | 44 |
| 103 | 75 | 80 | 38 |
| 90 | 73 | 63 | 33 |
| 81 | 71 | 49 | 27 |
| 75 | 66 | 38 | 22 |
| 67 | 15 | 10 |  |

Explain whether the range of measurements made by the student is suitable.
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A student uses a travelling microscope to investigate the perforation holes in a block of postage stamps.

The student positions the microscope to observe the line of perforation holes along the line XY shown in Figure 1.

Figure 1


Figure 2 shows the positions of the cross-wires of the microscope when the student makes readings $R_{1}, R_{2}$ and $R_{3}$.

Figure 2


The student's readings are shown in the table below.

| reading | position $/ \mathbf{m m}$ |
| :---: | :---: |
| $R_{1}$ | 25.51 |
| $R_{2}$ | 29.80 |
| $R_{3}$ | 31.82 |

(a) Determine the average separation $s$ between the centres of adjacent perforation holes along line $X Y$.
average separation $s=$ $\qquad$ mm
(b) State the precision of the microscope readings.
precision = $\qquad$ mm
(c) Determine the percentage uncertainty in your result for $s$.
percentage uncertainty =
$\qquad$ \%
(d) Determine the diameter $d$ of a perforation hole.

$$
\text { diameter } d=\ldots \mathrm{mm}
$$

(Total 6 marks)

