Figure 1


The system is suspended from one end of a thread passing over a pulley.
The other end of the thread is tied to a weight.
The system is shown in Figure 1 with the mass at the equilibrium position.
The spring constant (stiffness) is the same for each spring.
(a) Explain why the position of the fiducial mark shown in Figure 1 is suitable for this experiment.
$\qquad$
$\qquad$
$\qquad$
$\qquad$

The table below shows the measurements recorded by the student.

| Time for $\mathbf{2 0}$ oscillations of the mass-spring system/s |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 22.9 | 22.3 | 22.8 | 22.9 | 22.6 |

(b) (i) Determine the percentage uncertainty in these data.
percentage uncertainty $=$ $\qquad$
(ii) Determine the natural frequency of the mass-spring system.
natural frequency = $\qquad$
(c) The student connects the thread to a mechanical oscillator. The oscillator is set in motion using a signal generator and this causes the mass-spring system to undergo forced oscillations.

A vertical ruler is set up alongside the mass-spring system as shown in Figure 2. The student measures values of $A$, the amplitude of the oscillations of the mass as $f$, the frequency of the forcing oscillations, is varied.

Figure 2


A graph for the student's experiment is shown in Figure 3.
(i) Add a suitable scale to the frequency axis.

You should refer to your answer in part (b)(ii) and note that the scale starts at 0 Hz .
(ii) Deduce from Figure 3 the amplitude of the oscillations of $X$, the point where the mass-spring system is joined to the thread.
You should assume that the length of the thread is constant.
$\qquad$

Figure 3

(d) (i) State and explain how the student was able to determine the accurate shape of the graph in the region where $A$ is a maximum.
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$\qquad$
$\qquad$
$\qquad$
(ii) The student removes one of the springs and then repeats the experiment.

Add a new line to Figure 3 to show the graph the student obtains.
You may wish to use the equation $f=\frac{1}{2 \pi} \sqrt{\frac{k}{m}}$.

15 A stream of water flowing from a tap at a constant rate accelerates due to gravity. The stream becomes narrower the further it falls, before eventually breaking up into droplets.

An experiment is carried out to find out how $d$, the diameter of the stream of water, depends on $s$, the vertical distance the water has fallen. To avoid problems due to the effects of the tap outlet, $s$ is measured from a reference level below the outlet.

The arrangement used for the experiment is shown in Figure 1
Figure 1

(a) The distance $s$ is measured to the nearest mm using a vertical ruler.

The diameter $d$ is measured to the nearest 0.1 mm using a travelling microscope. Suggest why a travelling microscope was chosen to measure $d$ rather than vernier callipers.
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$\qquad$
(b) The data from the experiment suggest that $s=k d^{n}$ where $k$ is a constant and $n$ is an integer.

These data are used to plot the graph in Figure 2.
Figure 2

(i) Determine $n$ using Figure 2.
$n$ $\qquad$
(ii) Explain how the numerical value of $k$ can be obtained from Figure 2.
$\qquad$
$\qquad$
$\qquad$
(iii) Deduce the unit of $k$.
unit of $k=$

