2016 Newton

3 Fig. 3.1 shows a metal plate attached to the end of a spiral spring. The end **A** of the spring is fixed to a rigid clamp. The plate is pulled down by a small amount and released. The plate performs simple harmonic motion in a vertical plane at a natural frequency of 8 Hz and the spring remains in tension at all times.





(a) (i) On Fig. 3.2 sketch an acceleration *a* against displacement *x* graph for the motion of the metal plate. You are not required to give values on the axes.



Fig. 3.2

(ii) Explain how your graph could be used to determine the frequency of oscillation of the metal plate.

(b) Fig. 3.3 shows the variation of the vertical velocity v of the plate with time t at a frequency of 8 Hz.





Use the graph to determine

(i) the amplitude of the motion

amplitude = m [2]

(ii) the maximum vertical acceleration of the plate.

acceleration = ms⁻² [2]

(c) The metal plate is now immersed in light oil which provides a constant frictional force to the plate. On Fig. 3.4 draw carefully the graph you would expect to obtain for the variation of the vertical velocity v with time t. As a guide a copy of the graph in Fig. 3.3 is drawn for you.



Fig. 3.4

[2]

(d) The plate is now removed from the oil and the point **A** on the spring connected to an oscillator that vibrates vertically with constant amplitude. The frequency of the oscillator is increased slowly from 0 Hz to 12 Hz.

Describe and explain the motion of the metal plate during this procedure.

Sketch a labelled graph to help with your explanation.

In your answer, you should use appropriate technical terms spelled correctly.

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CW 2015

6 A student calculates the motion of a mass of 0.25 kg suspended by a spring of force constant 50 Nm^{-1} . The mass is displaced vertically from equilibrium by 0.030 m at time *t* = 0 and released.

The student uses $\Delta v = -\frac{k}{m} x \Delta t$ followed by $\Delta x = v \Delta t$ to estimate the displacement of the mass at time *t* = 0.10 s.

(a) Complete the table.

t/s	<i>v</i> /ms ⁻¹	<i>x</i> /m	∆ <i>t/</i> s	∆ <i>v</i> /ms ^{−1}
0.00	0.00	0.030	0.05	
0.05		0.015	0.05	-0.15
0.10	-0.45			
		1		

(b) The student uses the relationship $x = A\cos(2\pi ft)$ to calculate the displacement of the mass at t = 0.10 s as +0.0047 m.

Why is this value different from that obtained from the method of (a)?

[1]

oresse 2014

- 14 This question is about the article Simple pendulum experiment.
 - (a) A student obtains the following data for a pendulum of length 30 cm.

Time for 10 oscillations/s										
10.9	10.9	11.0	11.0	10.9	11.0	11.0	11.1	10.9	11.0	

(i) The student uses a stopwatch which records time to the nearest 0.01 s.She decides to quote the data to one decimal place.Give a reason for this choice.

[1]

(ii) State why measuring the time for 10 oscillations instead of one improves the quality of the results.

[1]

(iii) For the data above, the student correctly writes:

mean time for 10 oscillations = $11.0 \pm 0.1 s$.

Explain why the uncertainty in the period T is ± 0.01 s.

(iv) Show that a period $T = 1.10 \pm 0.01$ s leads to a value of

 $T^2 = 1.21 \pm 0.02 \,\mathrm{s}^2.$

[2]

(b) A second student times 10 oscillations for the range of lengths given in the table. He does not repeat the timing at each length.

L/m	Time for 10 oscillations/s	T/s	<i>T</i> ² /s ²
0.10	6.0		
0.15	7.9		
0.20	9.2	0.92	0.85
0.25	10.0	1.00	1.00
0.30	11.2	1.12	1.25
0.35	11.7	1.17	1.37
0.40	12.5	1.25	1.56

- (i) Complete the first two rows of the table, and use those data to complete the graph opposite. [2]
- (ii) Explain why the gradient of this graph should be

given that
$$\frac{4\pi^2}{g}$$

$$T = 2\pi \sqrt{\frac{L}{g}}$$

.



(iii) Use the graph to determine a value for g. Show your working clearly.

 $g = \dots m s^{-2}$ [3]

Question 14 continues on page 26

Turn over

(c) A third student suggests that the experiment could be improved by using pendulums of lengths between 2 m and 3 m.

Discuss the advantages and disadvantages of this suggestion.

[3]

[Total: 15]

END OF QUESTION PAPER