

Electric Fields

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Electric fields very similar to gravitational fields except attractive & repulsive.

$$\epsilon_0 = 8.85 \times 10^{-12} \text{ Fm}^{-1}$$

Again there are radial & constant fields.
Force between two charges that are point like

$$F = \frac{Q_1 Q_2}{4\pi\epsilon_0 r^2}$$

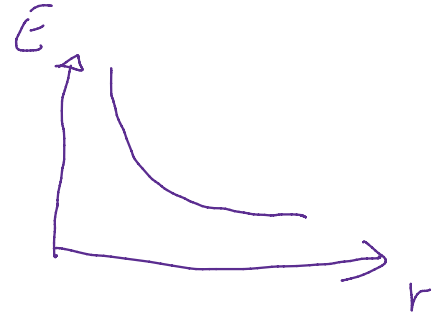
sometimes
 $\frac{1}{4\pi\epsilon_0} = k$

Electric Field strength

Force per unit charge \rightarrow the test charge = +1C. So effectively in the Force equation Q_2 has been set to +1C.

$E = \frac{F}{Q}$ in N/C Like g , E is a vector

we can therefore say $E = \frac{1}{4\pi\epsilon_0} \frac{Q}{r^2}$ where Q is the charge whose field the test charge is sitting in. This is another inverse square. $E \propto \frac{1}{r^2}$



Electric field strength in a uniform field

Often produced by two parallel plates connected to a pd - so lines

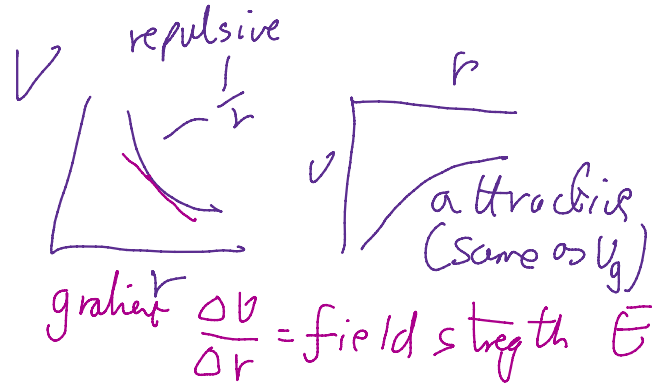
$$E = \frac{V}{d} \leftarrow \text{voltage } V/m \text{ or } N/C$$

Electric Potential (absolute potential) V

Potential energy - the potential energy per unit positive charge (that test charge again)

$$V = \frac{1}{4\pi\epsilon_0} \frac{Q}{r}$$

Sign depends on the sign of Q - the test charge is always positive
Like V_g this is the energy to move out to infinity.



Electric Potential Energy

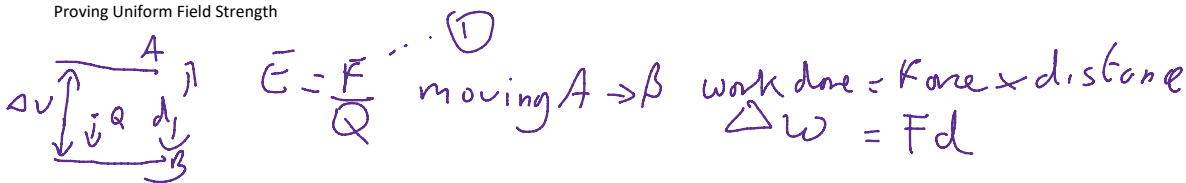
This is $V \times$ the second charge. So it's the energy to move a charge which doesn't happen to be exactly +1C

Electric Potential Difference

Work done in moving a charge between two potentials

$$\Delta W = Q \Delta V$$

Proving Uniform Field Strength



As $b \Delta W = Q \Delta V \therefore Q \Delta V = Fd \dots (2)$
 $\Rightarrow F = Q \frac{\Delta V}{d}$

from (1) $E Q = F \therefore E \cancel{Q} = Q \frac{\Delta V}{d} \Delta V = \text{p.d across plates} = V$

$$\text{div}(\vec{E}) = \rho = \frac{Q}{V}$$

$$\therefore \vec{E} = \frac{\Delta V}{\epsilon_0}$$

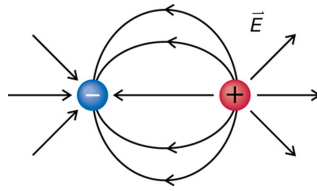
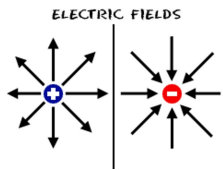
$$\Delta V = \frac{Q}{\epsilon_0} \frac{1}{d} = V$$

$$\therefore E = \frac{V}{d}$$

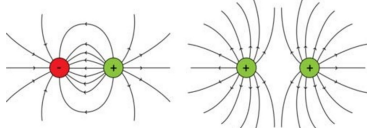
Equipotentials

For a point sphere equipotentials are spherical surfaces - you use on energy moving along a equipotential. For parallel plates they are straight lines.

Be aware of these diagrams



Interacting Electric Fields of Two Charged Particles:



Positively and Negatively Charged Particles

Two Positively Charged Particles