

Uncertainty and Error

24 January 2020 10:15

Absolute - the uncertainty in the measurement given as a fixed quantity - eg $2.4\text{cm} \pm 0.1\text{cm}$

Fractional - given as a fraction on the measurement $2.3\text{ cm} \pm 2/25$

Percentage - given as a percentage. Usually you have to convert from one of the others

Use Larger Readings...

Suppose you have meter and can measure to $\pm 0.1\text{ V}$

What is the % error on readings of 3V and 12V?

$$\begin{aligned} 3\text{V}: \% \text{ is } \frac{0.1}{3} \times 100 &= 3.3\% \quad \text{so } \Rightarrow 3\text{V} \pm 3.3\% \\ 12\text{V}: \% \text{ is } \frac{0.1}{12} \times 100 &= 0.8\% \quad \text{so } \Rightarrow 12\text{V} \pm 0.8\% \end{aligned}$$

Key here is that errors decrease on larger readings.

Errors on Means

Here are 5 repeated readings in Amps: 0.5, 0.3, 0.3, 0.3, 0.4

The range is largest - smallest = $0.5 - 0.3 = 0.2$

The error is half the range - in this case 0.1 so the mean is:

$0.36 \pm 0.1\text{V}$ which should be expressed as 0.4 ± 0.1

Combining Uncertainties

Often when putting numbers in to formulae you have errors on different quantities - so you have to follow these rules to combine the uncertainties.

Adding or Subtracting:

Add the **absolute** uncertainties

Multiplying or Dividing:

Add the **percentage** uncertainties

Raising to a power:

Multiply the **percentage** uncertainty by the power